

A review

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...of *almost* everything

I. Vectors

Pythagorus

$$a^2 + b^2 = c^2$$

Trig

sin, cos, tan,
sin⁻¹, cos⁻¹,
tan⁻¹

Needed to get the components or find
resultants

2. Kinematics

The way things move.

Displacement

$$\mathbf{x}$$

Velocity

$$\mathbf{v} = \frac{\Delta \mathbf{x}}{\Delta t}$$

Acceleration

$$\mathbf{a} = \frac{\Delta \mathbf{v}}{\Delta t}$$

2.1 Kinematic Equations

Velocity

$$\mathbf{v} = \mathbf{v}_0 + \mathbf{a}t$$

Displacement

$$\mathbf{x} = \bar{\mathbf{v}}t = \frac{\mathbf{v} + \mathbf{v}_0}{2}t$$

Displacement

$$\mathbf{x} = \mathbf{x}_0 + \mathbf{v}_0t + \frac{1}{2}\mathbf{a}t^2$$

Speed

$$v^2 = v_0^2 + 2a\Delta x$$

2.2 2-D kinematics

Motions happen in 2 dimensions. Treat these dimensions separately.

x-Displacement

$$\mathbf{x} = \mathbf{x}_0 + \mathbf{v}_{x0}t + \frac{1}{2}\mathbf{a}_x t^2$$

y-Displacement

$$\mathbf{y} = \mathbf{y}_0 + \mathbf{v}_{y0}t + \frac{1}{2}\mathbf{a}_y t^2$$

3. Forces

Newtons' Three Laws

$$\sum \mathbf{F} = m\mathbf{a}$$

3.3 Catalog of Forces

Pushing/pulling	General, non-descript interactions
Tension	Forces applied using ropes.
Gravity	Attractive force between <i>all</i> objects with mass
Normal	Interaction force - points perpendicular to plane of contact
Friction	A model to explain how surfaces interact
Drag	Velocity Dependent air resistance
Springs	Hooke's Law
Buoyancy Force	"The weight of the fluid displaced"

3.4 Gravity

Newton's Law of Gravitation $|\mathbf{F}_G| = \frac{Gm_1m_2}{r^2}$

little g $g = \frac{Gm_E}{R_E^2}$

weight (near surface of the earth) $\mathbf{F}_G = -mg$

3.5 Friction

static friction max $f_s^{\max} = \mu_s F_N$

kinetic friction $f_k = \mu_k F_N$

3.6 Springs

Hooke's Law / Restoring Force $\mathbf{F}_{spring} = -k\mathbf{x}$

4. Circular Motion

centripetal acceleration $a_c = \frac{v^2}{r}$

period / speed $v = \frac{2\pi r}{T}$

4.7 Work & Energy

work $W = Fs \cos \theta$

kinetic energy $KE = \frac{1}{2}mv^2$

potential energy $PE = mgh$

conservation of energy $W_{\text{NC}} = E_f - E_i$

4.8 Power

Power: change in energy per time

Find the rate of energy change

$$P = \frac{\Delta E}{\Delta t}$$

4.9 Impulse

Impulse $\mathbf{J} = \mathbf{F}\Delta t$

momentum $\mathbf{p} = m\mathbf{v}$

impulse-momentum $\mathbf{J} = \Delta\mathbf{p}$

And, momentum is always conserved.

5. Rotational Kinematics

Arc length

$$r\theta = s$$

angular displacement

$$\theta = \theta_0 + \omega_0 t + \frac{1}{2}\alpha t^2$$

angular velocity

$$\bar{\omega} = \frac{\Delta\theta}{\Delta t}$$

angular velocity

$$\omega^2 = \omega_0^2 + 2\alpha\theta$$

ω is a vector



5.10 Rotational

Arc length

$$r\theta = s$$

angular displacement

$$\theta = \theta_0 + \omega_0 t + \frac{1}{2}\alpha t^2$$

angular velocity

$$\bar{\omega} = \frac{\Delta\theta}{\Delta t}$$

angular velocity

$$\omega^2 = \omega_0^2 + 2\alpha\theta$$

5.11 Torque

Torque

$$\tau = rF \sin \phi$$

Moment of Inertia (point)

$$I = mr^2$$

Rotational 2nd law

$$\tau = I\alpha$$

Kinetic energy of rotation

$$KE_{\text{Rot}} = \frac{1}{2} I \omega^2$$

And, angular momentum is always conserved.

$$L = I\omega$$

6. Oscillations

General Restoring Force

$$\mathbf{F} = m\mathbf{a} = -\mathcal{O}\mathbf{x}$$

Solution: $x(t) = A \cos(\omega t + \phi)$

Mass on a spring

$$\omega = 2\pi f = \frac{2\pi}{T} = \sqrt{\frac{k}{m}}$$

Potential Energy

$$U_{\text{sp}} = \frac{1}{2} kx^2$$

Simple Pendulum

$$T = 2\pi \sqrt{\frac{L}{g}}$$

6.12 Simple Harmonic Motion

Position

$$x(t) = A \cos(\omega t)$$

Velocity

$$v(t) = -A\omega \sin(\omega t)$$

Acceleration

$$a(t) = -A\omega^2 \cos(\omega t)$$

Damping

$$x(t) = e^{-t/\tau} A \cos(\omega t + \phi)$$

7. Fluids

density

$$\rho = \frac{m}{V}$$

Pressure

$$P = \frac{F}{A}$$

Change in pressure due to depth

$$P_2 = P_1 + \rho gh$$

Archimedes' Principle.

$$F_B = W_{\text{fluid}}$$

7.13 Moving Fluids

Continuity

$$\rho_1 A_1 v_1 = \rho_2 A_2 v_2$$

Bernoulli

$$P_1 + \frac{1}{2}\rho v_1^2 + \rho g y_1 = P_2 + \frac{1}{2}\rho v_2^2 + \rho g y_2$$

8. Temperature and Heat

Thermal Contraction

$$\Delta L = \alpha L_0 \Delta T$$

Specific Heat

$$Q = cm\Delta T$$

Phase changes

$$Q = mL_F \text{ or } mL_V$$

Thermal Conductivity

$$Q = \frac{kA\Delta T t}{L}$$

9. Kinetic Theory

Ideal gas $PV = nRT = Nk_B T$

rms speed $v_{rms} = \sqrt{\frac{3k_B T}{m}}$

mean free path $\lambda = \frac{1}{\sqrt{2}\pi d^2 N/V}$

